

Dutch Lesson Study — Examples of Teacher Learning

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1. Lesson study

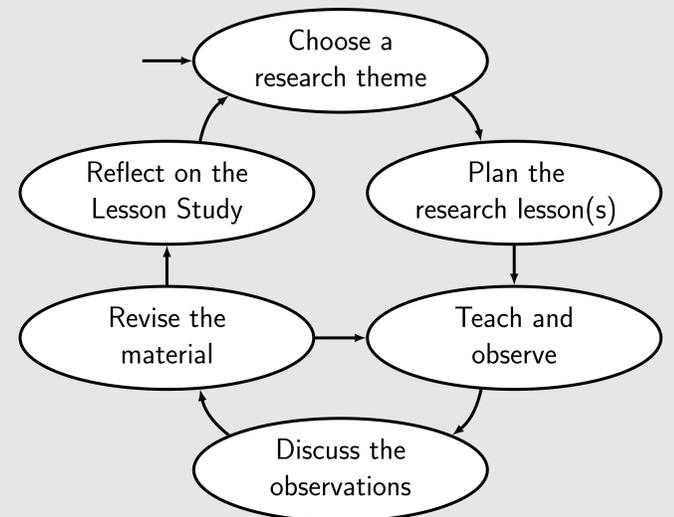
Lesson Study increases teachers' understanding of student learning by collaboratively

- **Planning** one or more lessons about a difficult topic;
- **Observing** one or more students live during these lessons in an actual class;
- **Discussing** the observations about student learning;
- **Revising** the material based on the observations.

Our Lesson Study goal: contribute to teachers' professional development through

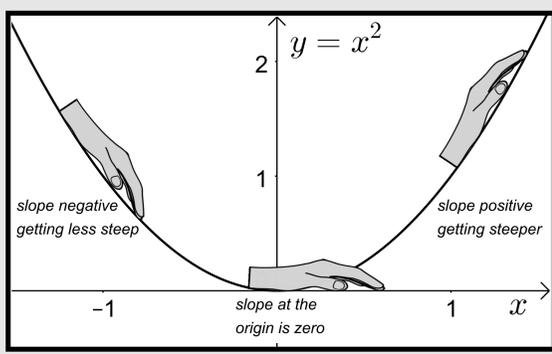
- Focus on subject matter and student learning (not on the teacher);
- Collaborative learning;
- Active involvement in curriculum design and development.

Our research goal: investigating the effects of Lesson Study on mathematics teachers' professional development.



Adapted from Stepanek et al. (2007).

2. Lesson Study example: the derivative



Adapted from Tall (2010).

Motivation:

- The **derivative** is very **important** in science and technology, but
- Students tend to use symbolic operations without **conceptual understanding**.

Findings:

- **Tracing** a graph using the teacher's hand gives the students a good conceptual understanding of **slope**.
- **Zooming in** on a graph (using GeoGebra) to show its "**local straightness**" is helpful for students' understanding of the derivative.

Verhoef, N.C., Coenders, F.G.M., Van Smaalen, D., Pieters, J.M., & Tall, D.O. (2015). *Professional development through lesson study: teaching the derivative using GeoGebra*. *Professional Development in Education*, 41(1).

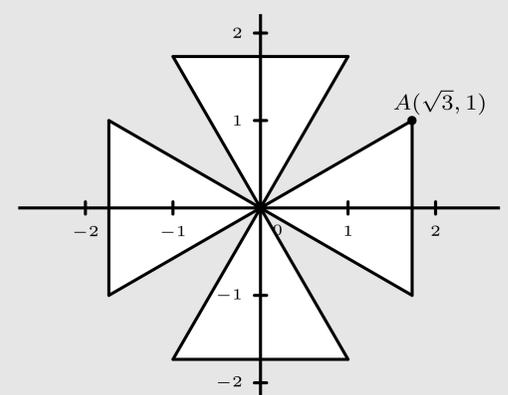
3. Lesson Study example: trigonometric functions

Motivation:

- The transition from **angle calculations** in triangles to the use of **trigonometric functions** easily confuses students.
- The teachers wanted the students to really understand the **symmetric properties** of sine and cosine.

Findings:

- The use of **icons** (windmill blades or a water wheel) elicits the use of symmetry, but care should be taken that students do not restrict their thinking to filling out coordinates.



Verhoef, N.C., & Timmer, M. (2013). *Lesson Study, deel 3 — ervaringen bij de introductie van periodieke bewegingen*. *Euclides*, 87(5).

4. Lesson Study example: combinatorial reasoning

		Can elements be repeated?	
		Yes	No
Does the order matter?	Yes	n^k	$\frac{n!}{(n-k)!}$
	No		$\binom{n}{k}$

Motivation: students often have great difficulties choosing between the use of **combinations**, **permutations** and **powers** when solving combinatorial problems.

Findings:

- Students really need to **visualise** each situation. **Acting out** a problem proved to provide more insight than the use of pictures.
- Coaching students to use their **common sense** and building up their confidence can be even more valuable for them than theoretical insight – this requires **active and involved teaching**.

Coenen T.J.M., Hof, F., & Verhoef, N.C. (2016). *Combinatorial reasoning to solve problems*. ICME 2016, Hamburg, Germany.
 Timmer, M., & Verhoef, N.C. (2014). *Combinatoriek: meer dan trucjes*. *Euclides*, 90(3).